

Regent Studies|www.regentstudies.com


## Prior Knowledge:

- Multiplication and division of whole numbers.



## Example 1:

Each bag of sweets in a shop contains 6 sweets. 3 are red, 2 are blue and 1 is yellow. How many red, blue and yellow sweets would I have if I bought 5 packets?

If I want to know how many sweets I would get from 2 packets, I multiply the numbers of sweets in 1 packet by 2.

In $\mathbf{2}$ packets, I would have $\mathbf{6}$ red, $\mathbf{4}$ blue and $\mathbf{2}$ yellow sweets.

If I want to know how many sweets I would get from 3 packets, I multiply the numbers of sweets in 1 packet by 3.

In 3 packets, I would have 9 red, 6 blue and 3 yellow sweets.

The question asks how many sweets I would have in 5 packets.
Therefore,
I multiply the numbers of sweets in 1 packet by 5.
In 5 packets, I would have 15 red, 10 blue and 5 yellow sweets.

## Example 2:

To make 5 tins of purple paint, you mix 2 tins of red paint with 3 tins of blue paint. How many tins of red paint do I need if I use 18 tins of blue paint?
There are two ways of answering this question. First, we can count up until we reach 18 tins of blue paint:

| Tins of purple <br> paint | Tins of red paint | Tins of blue paint |
| :---: | :---: | :---: |
| 5 | 2 | 3 |
| 10 | 4 | 6 |
| 15 | 6 | 9 |
| 20 | 8 | 12 |
| 25 | 10 | 15 |
| 30 | 12 | 18 |

As you can see, when we use 18 tins of blue paint, we need 12 tins of red paint.

## Example 2:

To make 5 tins of purple paint, you mix 2 tins of red paint with 3 tins of blue paint. How many tins of red paint do I need if I use 18 tins of blue paint?

We could also ask ourselves what we multiplied the original 3 tins of blue paint by to get 18 . We can find this by dividing 18 by 3:

$$
18 \div 3=6
$$

If we multiply the number of tins of blue paint by 6, we must also multiply the number of tins of red paint by 6:

$$
6 \times 2=12
$$

This gives us the same answer: we need 12 tins of red paint.

## Your Turn

1. A pencil case in a shop contains 5 pencils and 3 pens. How many pens would I get in 4 pencil cases?
2. A multi-pack of crisps contains 4 bags of ready-salted, 3 bags of cheese and onion and 2 bags of prawn cocktail. How many bags of prawn cocktail would I get in 7 multi-packs?
3. A 2-litre bottle of tropical drink contains the juice of $\mathbf{3}$ mangoes and 5 pineapples. How many pineapples do you need to make 8 litres of tropical drink?

## Your Turn

4. The table below shows the ingredients used at a bakery to make large cakes. Copy and complete the table. Make sure you state your units where necessary:

Cake Ingredients

| No. Cakes | Eggs | Flour | Sugar |
| :---: | :---: | :---: | :---: |
| 1 | 3 | 200 g |  |
| 2 |  |  | 300 g |
| 3 | 12 |  |  |
|  |  | 1600 g |  |
|  |  | 2 kg |  |
|  |  |  | 1.8 kg |

5. Marbles are put into bags in a factory. A bag contains 3 red marbles for each blue marble. If a bag contains $\mathbf{2 1}$ red marbles, how many blue marbles does it contain?
6. Students on a field trip are put into groups. Each group has one year 9 student, two year 8 students and three year 7 students. If there are 24 year 7s, how many year 8s are there?
7. A band sells 3 T-shirts for every 5 CDs. If they sold 25 CDs, how many T-shirts did they sell?
8. A cafe uses 3 rashers of bacon for every 2 sausages. One morning, they used 33 rashers of bacon. How many sausages did they use?
9. To make 5 litres of a shade of paint requires 3 litres of red paint and 2 litres of yellow. What is the maximum number of litres you can make if you have 12 litres of yellow paint?
10. Each time they perform an experiment, a scientist needs 5 bottles of chemical A and 7 bottles of chemical B. They have 30 bottles of chemical A and 40 bottles of chemical B. How many times can they do the experiment?
11. John is paid $£ 2$ for each $£ 3$ Mary is paid. Between them they are paid a total of $£ 40$. How much is John paid?
12. Ginny wins some money. Her daughter, Jo wins $£ 5$ for each $£ 20$ Ginny wins. If Jo gets $£ 55$, how much money did they win altogether?

Challenge:
The gears on a bike are set up so that when you pedal 2 full strokes, the rear wheel goes round 3 times. Each time the rear wheel goes round, the bike covers a distance of 2 m . Ann has to cycle 1.2 km home from school, uphill. How many full pedal strokes does she have to do to cover that distance?

## Answers

1. A pencil case in a shop contains 5 pencils and 3 pens. How many pens would I get in 4 pencil cases?
$4 \times 3=12$ pens
2. A multi-pack of crisps contains 4 bags of ready-salted, 3 bags of cheese and onion and 2 bags of prawn cocktail. How many bags of prawn cocktail would I get in 7 multi-packs?
$7 \times 2=14$ bags
3. A 2-litre bottle of tropical drink contains the juice of $\mathbf{3}$ mangoes and 5 pineapples. How many pineapples do you need to make 8 litres of tropical drink?
You need 4 lots of 2 litres to make 8 litres.
$4 \times 5=20$ pineapples

## Answers

4. The table below shows the ingredients used at a bakery to make large cakes. Copy and complete the table. Make sure you state your units where necessary:

## Cake Ingredients

| Cake Ingredients |  |  |  |
| :---: | :---: | :---: | :---: |
| No. Cakes | Eggs | Flour | Sugar |
| 1 | 3 | 200 g | 150 g |
| 2 | 6 | 400 g | 300 g |
| 3 | 9 | 600 g | 450 g |
| 4 | 12 | 800 g | 600 g |
| 5 | 15 | $1000 \mathrm{~g} / 1 \mathrm{~kg}$ | 750 g |
| 8 | 24 | 1600 g | $1200 \mathrm{~g} / 1.2 \mathrm{~kg}$ |
| 10 | 30 | 2 kg | $1500 \mathrm{~g} / 1.5 \mathrm{~kg}$ |
| 12 | 36 | $2400 \mathrm{~g} / 2.4 \mathrm{~kg}$ | 1.8 kg |

5. Marbles are put into bags in a factory. A bag contains 3 red marbles for each blue marble. If a bag contains 21 red marbles, how many blue marbles does it contain?
$21 \div 3=7$
$7 \times 1=7$
6. Students on a field trip are put into groups. Each group has one year 9 student, two year 8 students and three year 7 students. If there are 24 year 7s, how many year 8s are there?
$24 \div 3=8$
$8 \times 2=16$
7. A band sells $\mathbf{3}$ T-shirts for every $\mathbf{5}$ CDs. If they sold 25 CDs, how many T-shirts did they sell?
$25 \div 5=5$
$5 \times 3=15$ T-shirts
8. A cafe uses 3 rashers of bacon for every 2 sausages. One morning, they used 33 rashers of bacon. How many sausages did they use?
$33 \div 3=11$
$11 \times 2=22$
9. To make 5 litres of a shade of paint requires 3 litres of red paint and 2 litres of yellow. What is the maximum number of litres you can make if you have 12 litres of yellow paint?
$12 \div 2=6$
$6 \times 3=18$
$18+12=30$ litres
10. Each time they perform an experiment, a scientist needs 5 bottles of chemical A and 7 bottles of chemical B. They have 30 bottles of chemical A and 40 bottles of chemical B. How many times can they do the experiment?
$30 \div 5=6$ lots of chemical A
$40 \div 7=5 r 5$ or 5.7 lots of chemical B
They only have enough to do the experiment 5 times.
11. John is paid $£ 2$ for each $£ 3$ Mary is paid. Between them they are paid a total of $£ 40$. How much is John paid?
$2+3=5$
$40 \div 5=8$
$2 \times 8=£ 16$
12. Ginny wins some money. Her daughter, Jo wins $£ 5$ for each $£ 20$ Ginny wins. If Jo gets $£ 55$, how much money did they win altogether?
$55 \div 5=11$
$11 \times 20=£ 220$ (the amount Ginny wins)
$\mathbf{2 2 0} \mathbf{+ 5 5 = £ 2 7 5}$

Challenge:
The gears on a bike are set up so that when you pedal 2 full strokes, the rear wheel goes round 3 times. Each time the rear wheel goes round, the bike covers a distance of 2 m . Ann has to cycle 1.2 km home from school, uphill. How many full pedal strokes does she have to do to cover that distance?
$1.2 \mathrm{~km}=1200 \mathrm{~m}$
$1200 \div 2=600$ (the number of times the rear wheel goes round)
$600 \div 3=200$
$200 \times 2=400$ full pedal strokes


## Problems Involving the Relative Sizes of Two Quantities

## Prior Knowledge:

- Multiplication and division of whole numbers.


## Example 1:

Each bag of sweets in a shop contains 6 sweets. 3 are red, 2 are blue and 1 is yellow. How many red, blue and yellow sweets would I have if I bought 5 packets?

If I want to know how many sweets I would get from 2 packets, I multiply the numbers of sweets in 1 packet by 2.

In 2 packets, I would have 6 red, 4 blue and 2 yellow sweets.

If I want to know how many sweets I would get from 3 packets, I multiply the numbers of sweets in 1 packet by 3 .

In 3 packets, I would have 9 red, 6 blue and 3 yellow sweets.

The question asks how many sweets I would have in 5 packets. Therefore, I multiply the numbers of sweets in 1 packet by 5 .

In 5 packets, I would have $\mathbf{1 5}$ red, $\mathbf{1 0}$ blue and $\mathbf{5}$ yellow sweets.

## Example 2:

To make 5 tins of purple paint, you mix 2 tins of red paint with 3 tins of blue paint. How many tins of red paint do I need if I use 18 tins of blue paint?

There are two ways of answering this question. First, we can count up until we reach 18 tins of blue paint:

| Tins of purple paint | Tins of red paint | Tins of blue paint |
| :---: | :---: | :---: |
| 5 | 2 | 3 |
| 10 | 4 | 6 |
| 15 | 6 | 9 |
| 20 | 8 | 12 |
| 25 | 10 | 15 |
| $\mathbf{3 0}$ | $\mathbf{1 2}$ | $\mathbf{1 8}$ |

As you can see, when we use 18 tins of blue paint, we need 12 tins of red paint.

We could also ask ourselves what we multiplied the original 3 tins of blue paint by to get 18 . We can find this by dividing 18 by 3 :

$$
18 \div 3=6
$$

If we multiply the number of tins of blue paint by 6 , we must also multiply the number of tins of red paint by 6 :

$$
6 \times 2=12
$$

This gives us the same answer: we need 12 tins of red paint.

## Problems Involving the Relative Sizes of Two Quantities Worksheet

1. A pencil case in a shop contains 5 pencils and 3 pens. How many pens would I get in 4 pencil cases?
2. A multi-pack of crisps contains 4 bags of ready-salted, 3 bags of cheese and onion and 2 bags of prawn cocktail. How many bags of prawn cocktail would I get in 7 multi-packs?
3. A 2-litre bottle of tropical drink contains the juice of 3 mangoes and 5 pineapples. How many pineapples do you need to make 8 litres of tropical drink?
4. The table below shows the ingredients used at a bakery to make large cakes. Copy and complete the table. Make sure you state your units where necessary:

| Cake Ingredients |  |  | Flour |
| :--- | :--- | :--- | :--- |
| No. Cakes | Eggs | 200 g | Sugar |
| 1 | 3 |  |  |
| 2 |  |  | 300 g |
| 3 | 12 |  |  |
|  |  | 1600 g | 750 g |
|  |  | 2 kg |  |
|  |  |  |  |
|  |  | 1.8 kg |  |

5. Marbles are put into bags in a factory. A bag contains 3 red marbles for each blue marble. If a bag contains 21 red marbles, how many blue marbles does it contain?
6. Students on a field trip are put into groups. Each group has one year 9 student, two year 8 students and three year 7 students. If there are 24 year 7 s , how many year 8 s are there?
7. A band sells 3 T-shirts for every 5 CDs. If they sold 25 CDs, how many T-shirts did they sell?
8. A cafe uses 3 rashers of bacon for every 2 sausages. One morning, they used 33 rashers of bacon. How many sausages did they use?
9. To make 5 litres of a shade of paint requires 3 litres of red paint and 2 litres of yellow. What is the maximum number of litres you can make if you have 12 litres of yellow paint?
10. Each time they perform an experiment, a scientist needs 5 bottles of chemical $A$ and 7 bottles of chemical B. They have 30 bottles of chemical A and 40 bottles of chemical B. How many times can they do the experiment?
11. John is paid $£ 2$ for each $£ 3$ Mary is paid. Between them they are paid a total of $£ 40$. How much is John paid?
12. Ginny wins some money. Her daughter, Jo wins $£ 5$ for each $£ 20$ Ginny wins. If Jo gets $£ 55$, how much money did they win altogether?

## Challenge:

The gears on a bike are set up so that when you pedal 2 full strokes, the rear wheel goes round 3 times. Each time the rear wheel goes round, the bike covers a distance of 2 m . Ann has to cycle 1.2 km home from school, uphill. How many full pedal strokes does she have to do to cover that distance?

## Problems Involving the Relative Sizes of Two Quantities Worksheet

1. A pencil case in a shop contains 5 pencils and 3 pens. How many pens would I get in 4 pencil cases?
$\qquad$
2. A multi-pack of crisps contains 4 bags of ready-salted, 3 bags of cheese and onion and 2 bags of prawn cocktail. How many bags of prawn cocktail would I get in 7 multi-packs?
$\qquad$
3. A 2-litre bottle of tropical drink contains the juice of 3 mangoes and 5 pineapples. How many pineapples do you need to make 8 litres of tropical drink?
$\qquad$
$\qquad$
4. The table below shows the ingredients used at a bakery to make large cakes. Fill in the gaps. Make sure you state your units where necessary:

| Cake Ingredients |  |  |  |
| :--- | :--- | :--- | :--- |
| No. Cakes | Eggs | Flour | Sugar |
| 1 | 3 | 200 g |  |
| 2 |  |  | 300 g |
| 3 | 12 |  |  |
|  |  |  | 750 g |
|  |  | 2 kg |  |
|  |  |  | 1.8 kg |

5. Marbles are put into bags in a factory. A bag contains 3 red marbles for each blue marble. If a bag contains 21 red marbles, how many blue marbles does it contain?
6. Students on a field trip are put into groups. Each group has one year 9 student, two year 8 students and three year 7 students. If there are 24 year 7 s , how many year 8 s are there?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
7. A band sells 3 T-shirts for every 5 CDs. If they sold 25 CDs, how many T-shirts did they sell?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
8. A cafe uses 3 rashers of bacon for every 2 sausages. One morning, they used 33 rashers of bacon. How many sausages did they use?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
9. To make 5 litres of a shade of paint requires 3 litres of red paint and 2 litres of yellow. What is the maximum number of litres you can make if you have 12 litres of yellow paint?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
10. Each time they perform an experiment, a scientist needs 5 bottles of chemical $A$ and 7 bottles of chemical B. They have 30 bottles of chemical A and 40 bottles of chemical B. How many times can they do the experiment?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
11. John is paid $£ 2$ for each $£ 3$ Mary is paid. Between them they are paid a total of $£ 40$. How much is John paid?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
12. Ginny wins some money. Her daughter, Jo wins $£ 5$ for each $£ 20$ Ginny wins. If Jo gets $£ 55$, how much money did they win altogether?
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Challenge:

The gears on a bike are set up so that when you pedal 2 full strokes, the rear wheel goes round 3 times. Each time the rear wheel goes round, the bike covers a distance of 2 m . Ann has to cycle 1.2 km home from school, uphill. How many full pedal strokes does she have to do to cover that distance?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Problems Involving the Relative Sizes of Two Quantities Answers

1. A pencil case in a shop contains 5 pencils and 3 pens. How many pens would I get in 4 pencil cases?
$4 \times 3=12$ pens
2. A multi-pack of crisps contains 4 bags of ready-salted, 3 bags of cheese and onion and 2 bags of prawn cocktail. How many bags of prawn cocktail would I get in 7 multi-packs?
$7 \times 2=14$ bags
3. A 2-litre bottle of tropical drink contains the juice of 3 mangoes and 5 pineapples. How many pineapples do you need to make 8 litres of tropical drink?
You need 4 lots of 2 litres to make 8 litres.
$4 \times 5=20$ pineapples
4. The table below shows the ingredients used at a bakery to make large cakes. Fill in the gaps. Make sure you state your units where necessary:

Cake Ingredients

| No. Cakes | Eggs | Flour | Sugar |
| :--- | :--- | :--- | :--- |
| 1 | 3 | 200 g | $\mathbf{1 5 0 g}$ |
| 2 | 6 | $\mathbf{4 0 0 g}$ | 300 g |
| 3 | 9 | $\mathbf{6 0 0 g}$ | $\mathbf{4 5 0 g}$ |
| $\mathbf{4}$ | 12 | 800 g | $\mathbf{6 0 0 \mathrm { g }}$ |
| $\mathbf{5}$ | $\mathbf{1 5}$ | $\mathbf{1 0 0 0 \mathrm { g } / 1 \mathrm { kg }}$ | 750 g |
| 8 | $\mathbf{2 4}$ | 1600 g | $\mathbf{1 2 0 0 \mathrm { g } / 1 . 2 \mathrm { kg }}$ |
| $\mathbf{1 0}$ | 30 | 2 kg | $\mathbf{1 5 0 0 \mathrm { g } / 1 . 5 \mathrm { kg }}$ |
| $\mathbf{1 2}$ | $\mathbf{3 6}$ | $\mathbf{2 4 0 0 \mathrm { g } / \mathbf { 2 . 4 k g }}$ | 1.8 kg |

5. Marbles are put into bags in a factory. A bag contains 3 red marbles for each blue marble. If a bag contains 21 red marbles, how many blue marbles does it contain?
$21 \div 3=7$
$7 \times 1=7$
6. Students on a field trip are put into groups. Each group has one year 9 student, two year 8 students and three year 7 students. If there are 24 year 7 s , how many year 8 s are there?
$24 \div 3=8$
$8 \times 2=16$
7. A band sells 3 T-shirts for every 5 CDs. If they sold 25 CDs, how many T-shirts did they sell?
$25 \div 5=5$
$5 \times 3=15$ T-shirts
8. A cafe uses 3 rashers of bacon for every 2 sausages. One morning, they used 33 rashers of bacon. How many sausages did they use?
$33 \div 3=11$
$11 \times 2=22$
9. To make 5 litres of a shade of paint requires 3 litres of red paint and 2 litres of yellow. What is the maximum number of litres you can make if you have 12 litres of yellow paint?
$12 \div \mathbf{2}=\mathbf{6}$
$6 \times 3=18$
$18+12=30$ litres
10. Each time they perform an experiment, a scientist needs 5 bottles of chemical $A$ and 7 bottles of chemical B. They have 30 bottles of chemical A and 40 bottles of chemical B. How many times can they do the experiment?
$30 \div 5=\mathbf{6}$ lots of chemical A
$40 \div 7=5 r 5$ or 5.7 lots of chemical B
They only have enough to do the experiment 5 times.
11. John is paid $£ 2$ for each $£ 3$ Mary is paid. Between them they are paid a total of $£ 40$. How much is John paid?
$2+3=5$
$40 \div 5=8$
$2 \times 8=£ 16$
12. Ginny wins some money. Her daughter, Jo wins $£ 5$ for each $£ 20$ Ginny wins. If Jo gets $£ 55$, how much money did they win altogether?
$55 \div 5=11$
$11 \times 20=£ 220$ (the amount Ginny wins)
$\mathbf{2 2 0} \mathbf{+ 5 5 = £ 2 7 5}$

## Challenge:

The gears on a bike are set up so that when you pedal 2 full strokes, the rear wheel goes round 3 times. Each time the rear wheel goes round, the bike covers a distance of 2 m . Ann has to cycle 1.2 km home from school, uphill. How many full pedal strokes does she have to do to cover that distance?
$1.2 \mathrm{~km}=1200 \mathrm{~m}$
$1200 \div \mathbf{2}=600$ (the number of times the rear wheel goes round)
$600 \div \mathbf{3}=\mathbf{2 0 0}$
$200 \times 2=400$ full pedal strokes

