



# **Prior Knowledge:**

• Multiplication and division of whole numbers.



## **Example 1**:

Each bag of sweets in a shop contains 6 sweets. 3 are red, 2 are blue and 1 is yellow. How many red, blue and yellow sweets would I have if I bought 5 packets?

If I want to know how many sweets I would get from 2 packets, I multiply the numbers of sweets in 1 packet by 2. In 2 packets, I would have 6 red, 4 blue and 2 yellow sweets.

If I want to know how many sweets I would get from 3 packets, I multiply the numbers of sweets in 1 packet by 3. In 3 packets, I would have 9 red, 6 blue and 3 yellow sweets.

The question asks how many sweets I would have in 5 packets. Therefore,

I multiply the numbers of sweets in 1 packet by 5. In 5 packets, I would have 15 red, 10 blue and 5 yellow sweets.

## **Example 2:**

To make 5 tins of purple paint, you mix 2 tins of red paint with 3 tins of blue paint. How many tins of red paint do I need if I use 18 tins of blue paint?

There are two ways of answering this question. First, we can count up until we reach 18 tins of blue paint:

Tins of purple paint	Tins of red paint	Tins of blue paint
5	2	3
10	4	6
15	6	9
20	8	12
25	10	15
30	12	18

As you can see, when we use 18 tins of blue paint, we need 12 tins of red paint.

## **Example 2:**

To make 5 tins of purple paint, you mix 2 tins of red paint with 3 tins of blue paint. How many tins of red paint do I need if I use 18 tins of blue paint?

We could also ask ourselves what we multiplied the original 3 tins of blue paint by to get 18. We can find this by dividing 18 by 3:

 $18 \div 3 = 6$ 

If we multiply the number of tins of blue paint by 6, we must also multiply the number of tins of red paint by 6:

6 × 2 = 12

This gives us the same answer: we need 12 tins of red paint.



- 1. A pencil case in a shop contains 5 pencils and 3 pens. How many pens would I get in 4 pencil cases?
- 2. A multi-pack of crisps contains 4 bags of ready-salted, 3 bags of cheese and onion and 2 bags of prawn cocktail. How many bags of prawn cocktail would I get in 7 multi-packs?
- 3. A 2-litre bottle of tropical drink contains the juice of 3 mangoes and 5 pineapples. How many pineapples do you need to make 8 litres of tropical drink?

## **Your Turn**

The table below shows the ingredients used at a bakery to make large cakes.
 Copy and complete the table. Make sure you state your units where necessary:

No. Cakes	Eggs	Flour	Sugar
1	3	200g	
2	1.2		300g
3			
	12		2252
			750g
		1600g	
		2kg	States and
			1.8kg

## **Your Turn**

- 5. Marbles are put into bags in a factory. A bag contains 3 red marbles for each blue marble. If a bag contains 21 red marbles, how many blue marbles does it contain?
- 6. Students on a field trip are put into groups. Each group has one year 9 student, two year 8 students and three year 7 students. If there are 24 year 7s, how many year 8s are there?
- 7. A band sells 3 T-shirts for every 5 CDs. If they sold 25 CDs, how many T-shirts did they sell?
- 8. A cafe uses 3 rashers of bacon for every 2 sausages. One morning, they used 33 rashers of bacon. How many sausages did they use?
- 9. To make 5 litres of a shade of paint requires 3 litres of red paint and 2 litres of yellow. What is the maximum number of litres you can make if you have 12 litres of yellow paint?

## **Your Turn**

- 10. Each time they perform an experiment, a scientist needs 5 bottles of chemical A and 7 bottles of chemical B. They have 30 bottles of chemical A and 40 bottles of chemical B. How many times can they do the experiment?
- 11. John is paid £2 for each £3 Mary is paid. Between them they are paid a total of £40. How much is John paid?
- 12. Ginny wins some money. Her daughter, Jo wins £5 for each £20 Ginny wins. If Jo gets £55, how much money did they win altogether?

## Challenge:

The gears on a bike are set up so that when you pedal 2 full strokes, the rear wheel goes round 3 times. Each time the rear wheel goes round, the bike covers a distance of 2m. Ann has to cycle 1.2km home from school, uphill. How many full pedal strokes does she have to do to cover that distance?



- A pencil case in a shop contains 5 pencils and 3 pens. How many pens would I get in 4 pencil cases?
  - 4 × 3 = 12 pens
- 2. A multi-pack of crisps contains 4 bags of ready-salted, 3 bags of cheese and onion and 2 bags of prawn cocktail. How many bags of prawn cocktail would I get in 7 multi-packs?
  - 7 × 2 = 14 bags
- 3. A 2-litre bottle of tropical drink contains the juice of 3 mangoes and 5 pineapples. How many pineapples do you need to make 8 litres of tropical drink?

You need 4 lots of 2 litres to make 8 litres.

4 × 5 = 20 pineapples

4. The table below shows the ingredients used at a bakery to make large cakes. Copy and complete the table. Make sure you state your units where necessary:

Cake Ingredients			
No. Cakes	Eggs	Flour	Sugar
1	3	200g	150g
2	6	400g	300g
3	9	600g	450g
4	12	800g	600g
5	15	1000g/1kg	750g
8	24	1600g	1200g/1.2kg
10	30	2kg	1500g/1.5kg
12	36	2400g/2.4kg	1.8kg

- Marbles are put into bags in a factory. A bag contains 3 red marbles for each blue marble. If a bag contains 21 red marbles, how many blue marbles does it contain?
   21 ÷ 3 = 7
  - 7 × 1 = 7
- 6. Students on a field trip are put into groups. Each group has one year 9 student, two year 8 students and three year 7 students. If there are 24 year 7s, how many year 8s are there?

24 ÷ 3 = 8 8 × 2 = 16

- 7. A band sells 3 T-shirts for every 5 CDs. If they sold 25 CDs, how many T-shirts did they sell?
  25 ÷ 5 = 5
  5 × 3 = 15 T-shirts
- 8. A cafe uses 3 rashers of bacon for every 2 sausages. One morning, they used 33 rashers of bacon. How many sausages did they use?
  33 ÷ 3 = 11
  11 × 2 = 22

- 9. To make 5 litres of a shade of paint requires 3 litres of red paint and 2 litres of yellow. What is the maximum number of litres you can make if you have 12 litres of yellow paint?
  12 ÷ 2 = 6
  6 × 3 = 18
  - 18 + 12 = 30 litres
- 10. Each time they perform an experiment, a scientist needs 5 bottles of chemical A and 7 bottles of chemical B. They have 30 bottles of chemical A and 40 bottles of chemical B. How many times can they do the experiment?
  30 ÷ 5 = 6 lots of chemical A
  40 ÷ 7 = 5r5 or 5.7 lots of chemical B
  They only have enough to do the experiment 5 times.
- 11. John is paid £2 for each £3 Mary is paid. Between them they are paid a total of £40. How much is John paid?
  - 2 + 3 = 5
  - 40 ÷ 5 = 8
  - $2 \times 8 = \pm 16$

12. Ginny wins some money. Her daughter, Jo wins £5 for each £20 Ginny wins. If Jo gets £55, how much money did they win altogether? 55 ÷ 5 = 11 11 × 20 = £220 (the amount Ginny wins) 220 + 55 = £275

## **Challenge:**

The gears on a bike are set up so that when you pedal 2 full strokes, the rear wheel goes round 3 times. Each time the rear wheel goes round, the bike covers a distance of 2m. Ann has to cycle 1.2km home from school, uphill. How many full pedal strokes does she have to do to cover that distance? 1.2km = 1200m 1200  $\div$  2 = 600 (the number of times the rear wheel goes round) 600  $\div$  3 = 200 200  $\times$  2 = 400 full pedal strokes



## **Problems Involving the Relative Sizes of Two Quantities**

### **Prior Knowledge:**

• Multiplication and division of whole numbers.

### Example 1:

Each bag of sweets in a shop contains 6 sweets. 3 are red, 2 are blue and 1 is yellow. How many red, blue and yellow sweets would I have if I bought 5 packets?

If I want to know how many sweets I would get from 2 packets, I multiply the numbers of sweets in 1 packet by 2.

In 2 packets, I would have 6 red, 4 blue and 2 yellow sweets.

If I want to know how many sweets I would get from 3 packets, I multiply the numbers of sweets in 1 packet by 3.

In 3 packets, I would have 9 red, 6 blue and 3 yellow sweets.

The question asks how many sweets I would have in 5 packets. Therefore, I multiply the numbers of sweets in 1 packet by 5.

In 5 packets, I would have **15 red, 10 blue and 5 yellow sweets**.

### Example 2:

To make 5 tins of purple paint, you mix 2 tins of red paint with 3 tins of blue paint. How many tins of red paint do I need if I use 18 tins of blue paint?

There are two ways of answering this question. First, we can count up until we reach 18 tins of blue paint:

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As you can see, when we use 18 tins of blue paint, we need **12 tins of red paint**.

We could also ask ourselves what we multiplied the original 3 tins of blue paint by to get 18. We can find this by dividing 18 by 3:

18 ÷ 3 = 6

If we multiply the number of tins of blue paint by 6, we must also multiply the number of tins of red paint by 6:

6 × 2 = 12

This gives us the same answer: we need **12 tins of red paint**.

## Problems Involving the Relative Sizes of Two Quantities **Worksheet**

- 1. A pencil case in a shop contains 5 pencils and 3 pens. How many pens would I get in 4 pencil cases?
- 2. A multi-pack of crisps contains 4 bags of ready-salted, 3 bags of cheese and onion and 2 bags of prawn cocktail. How many bags of prawn cocktail would I get in 7 multi-packs?
- 3. A 2-litre bottle of tropical drink contains the juice of 3 mangoes and 5 pineapples. How many pineapples do you need to make 8 litres of tropical drink?
- 4. The table below shows the ingredients used at a bakery to make large cakes. Copy and complete the table. Make sure you state your units where necessary:

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			750g
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			1.8kg

- 5. Marbles are put into bags in a factory. A bag contains 3 red marbles for each blue marble. If a bag contains 21 red marbles, how many blue marbles does it contain?
- 6. Students on a field trip are put into groups. Each group has one year 9 student, two year 8 students and three year 7 students. If there are 24 year 7s, how many year 8s are there?
- 7. A band sells 3 T-shirts for every 5 CDs. If they sold 25 CDs, how many T-shirts did they sell?
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## Challenge:

The gears on a bike are set up so that when you pedal 2 full strokes, the rear wheel goes round 3 times. Each time the rear wheel goes round, the bike covers a distance of 2m. Ann has to cycle 1.2km home from school, uphill. How many full pedal strokes does she have to do to cover that distance?

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### Problems Involving the Relative Sizes of Two Quantities Worksheet

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# Problems Involving the Relative Sizes of Two Quantities **Answers**

1. A pencil case in a shop contains 5 pencils and 3 pens. How many pens would I get in 4 pencil cases?

## 4 × 3 = 12 pens

2. A multi-pack of crisps contains 4 bags of ready-salted, 3 bags of cheese and onion and 2 bags of prawn cocktail. How many bags of prawn cocktail would I get in 7 multi-packs?

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12 ÷ 2 = 6 6 × 3 = 18 18 + 12 = 30 litres

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1.2km = 1200m 1200 ÷ 2 = 600 (the number of times the rear wheel goes round) 600 ÷ 3 = 200 200 × 2 = 400 full pedal strokes